

Nome: _____ Cognome: _____ Matr: _____ Postazione _____

Write a program using the C language (name the project with your student ID) that behaves as described below. The available time is 120 minutes. At the end of the time, the saved files on **U:** are going to be automatically collected. Additional documents, files... are available in **T:\Bertozzi**, and it is recommended to use WordPad to read text files.

We want to develop a C program to calculate all prime numbers within an interval $[1, n]$.

To do this:

1. Define a dynamically allocated array of unsigned int initially empty.
2. Ask the user for an integer $n > 1$.
3. For all numbers x from 1 to n , invoke the function $ferm(x)$ which returns the number of prime divisors of the number passed as an argument. If this function returns 2, increase the size of the array defined in step #1 and add the number x to that array.
4. Implement the recursive function **unsigned int ferm(unsigned int n)** which performs the following steps:
 - a) If n equals 0, return 0
 - b) If n equals 1, return 1
 - c) If n is even, return $1 + ferm(n/2)$
 - d) Alternatively, define three integer support variables: a , b , and $b2$.
 - a is initialized with the ceiling approximation of the square root of n .
 - $b2$ is initialized with $a \times a - n$.
 - b is initialized with the integer part of the square root of $b2$.
 - Until $b2$ is not a perfect square, increase a and recalculate the values of b and $b2$ as indicated.
 - at the end of the loop, if $a + b$ equals n , the function returns 2, otherwise returns $1 + ferm(a + b)$.
5. The program ends by printing how many prime numbers are present in the interval $[1, n]$ and their respective values.

The code should be developed following the proposed order. Correction ends at the first point not correctly implemented.

In order to develop point #3, initially define an empty stub for the function ferm() which returns a preset value so that point #3 can be tested.

Take into account the risk of overflow for variables a , b , and especially $b2$.

Refer to the manual to understand what the function `double ceil(double x)` does.